

Normals

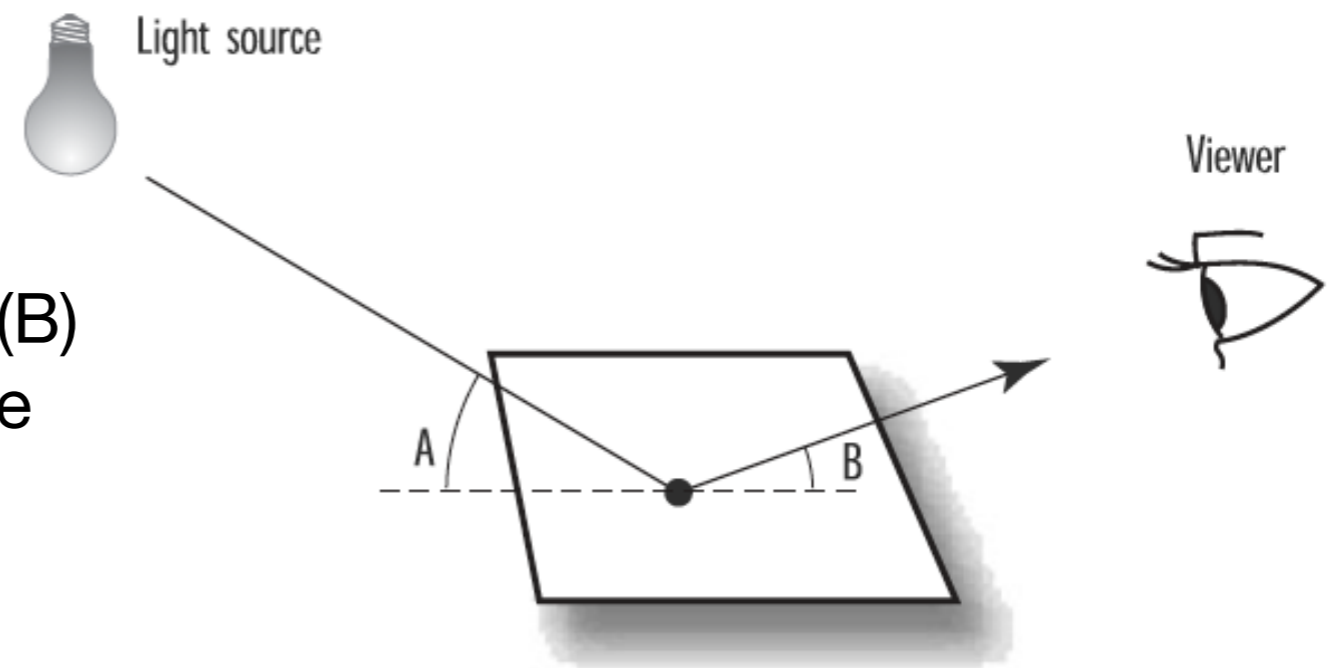
OpenGL

Which Way is Up?

- When you specify a light source, tell OpenGL where it is and in which direction it's shining.
- Often, the light source shines in all directions, but it can be directional.
- Either way, for any object, the rays of light from any source (other than a pure ambient source) strike the surface of the polygons that make up the object at an angle.
- In the case of a directional light, the surfaces of all polygons might not necessarily be illuminated.
- To calculate the shading effects across the surface of the polygons, OpenGL must be able to calculate the angle.

Angles

- A polygon (a square) is being struck by a ray of light from some source.
- The ray makes an angle (A) with the plane as it strikes the surface.
- The light is then reflected at an angle (B) toward the viewer (or you wouldn't see it).
- These angles are used by OpenGL in conjunction with the lighting and material properties to calculate the apparent color of that location

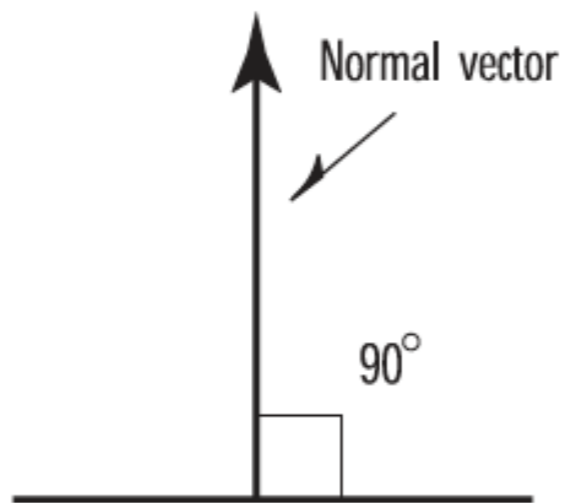


Calculating the Angles?

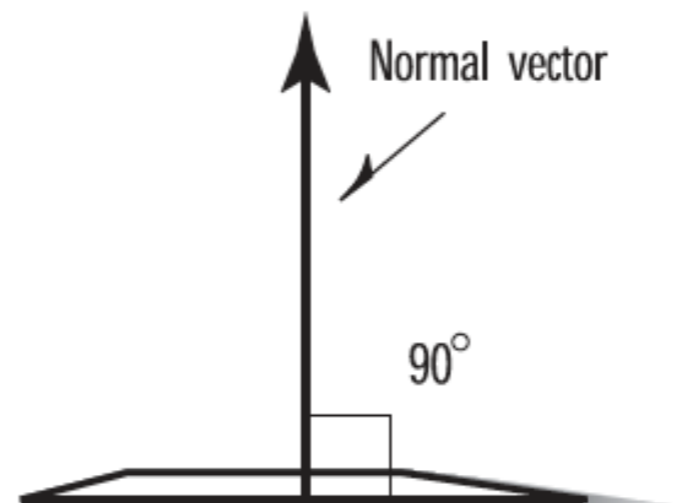
- From a programming standpoint, these lighting calculations present a slight conceptual difficulty.
- Each polygon is created as a set of vertices, and each vertex is then struck by a ray of light at some angle.
- How to calculate the angle between a point and a line (the ray of light)?
- Can't geometrically find the angle between a single point and a line in 3D space because there are an infinite number of possibilities.
- Therefore, you must associate with each vertex some piece of information that denotes a direction upward from the vertex and away from the surface of the primitive.

Surface Normals

- A line from the vertex in the upward direction starts in some imaginary plane at a right angle.
- This line is called a normal vector.
- The imaginary plane is the surface of the polygon



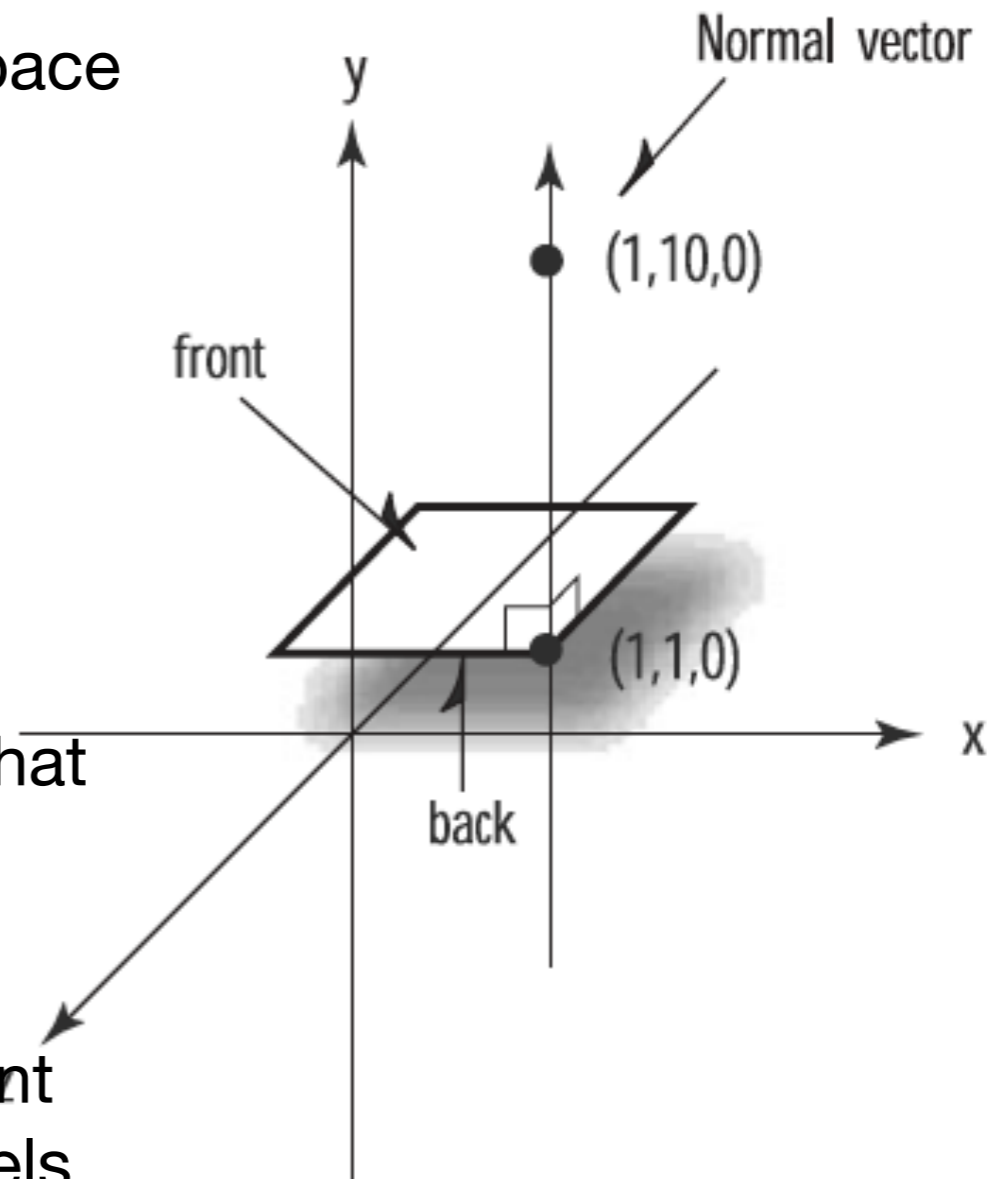
A 2D normal vector



A 3D normal vector

Specifying Normals

- Eg a plane floating above the xz plane in 3D space
- The line through the vertex $(1,1,0)$ that is perpendicular to the plane.
- Select a point on this line, say $(1,10,0)$, the line from the first point $(1,1,0)$ to the second point $(1,10,0)$ is our normal vector.
- The second point specified actually indicates that the direction from the vertex is up in the y direction.
- This convention is also used to indicate the front and back sides of polygons, as the vector travels up and away from the front surface.

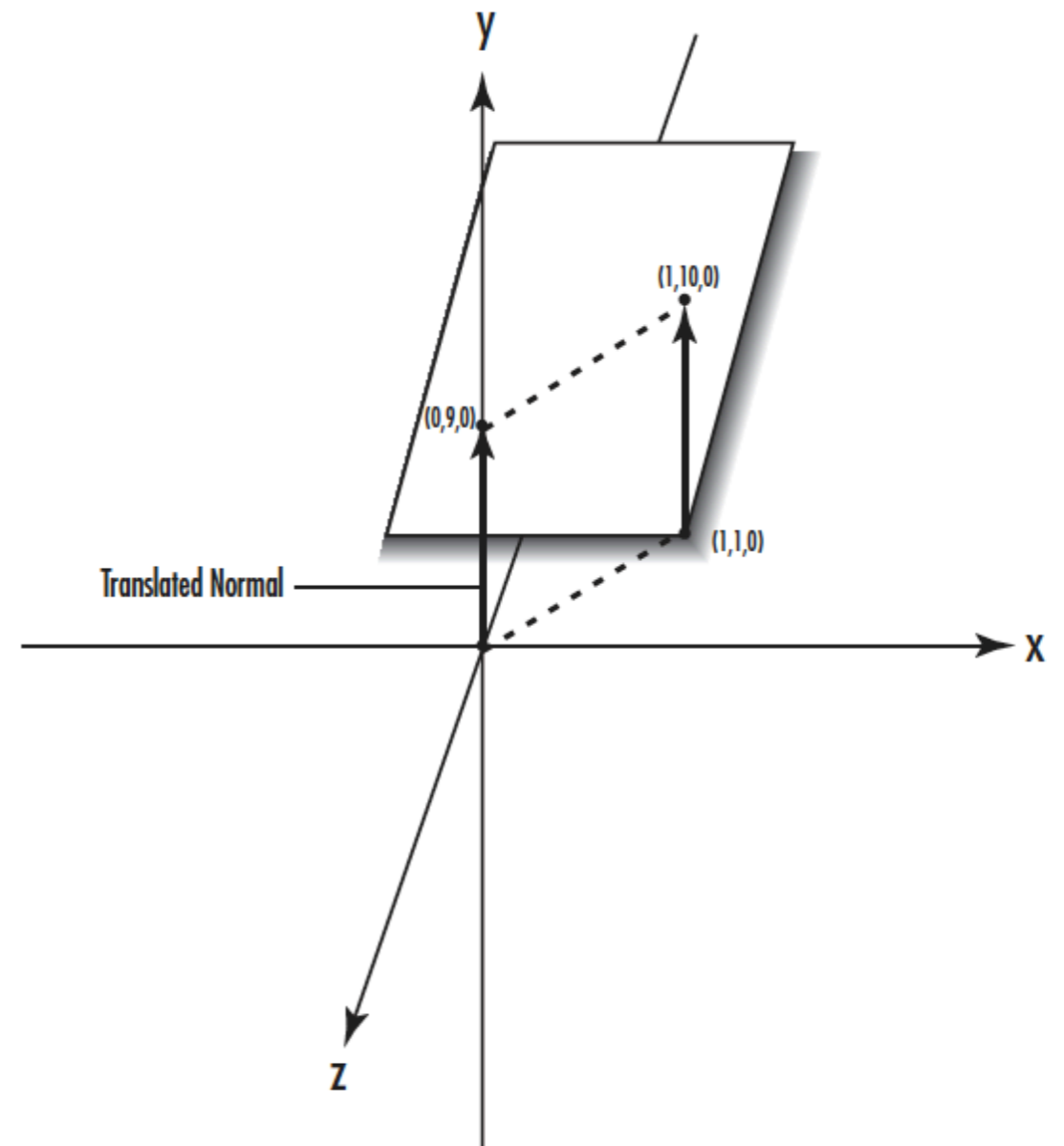


Normal Vector

- This second point is the number of units in the x, y, and z directions for some point on the normal vector away from the vertex.
- Rather than specify two points for each normal vector, we can subtract the vertex from the second point on the normal, yielding a single coordinate triplet that indicates the x, y, and z steps away from the vertex.
- For our example, this is $(1, 10, 0) - (1, 1, 0) = (1 - 1, 10 - 1, 0) = (0, 9, 0)$

Normalised

- If the vertex were translated to the origin, the point specified by subtracting the two original points would still specify the direction pointing away and at a 90° angle from the surface.
- The vector is a directional quantity that tells OpenGL which direction the vertices (or polygon) face

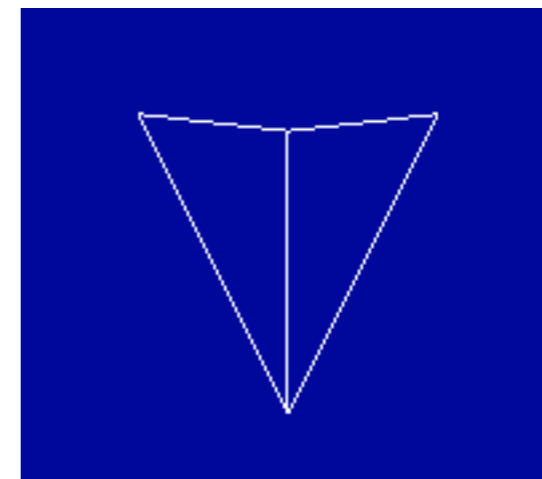


Specifying Normals to OpenGL

- The function `glNormal3f` takes the coordinate triplet that specifies a normal vector pointing in the direction perpendicular to the surface of this triangle.
- Here, the normals for all three vertices have the same direction, which is down the negative y-axis.
- A simple example because the triangle is lying flat in the xz plane, and it actually represents part of the nose cone of our model jet.

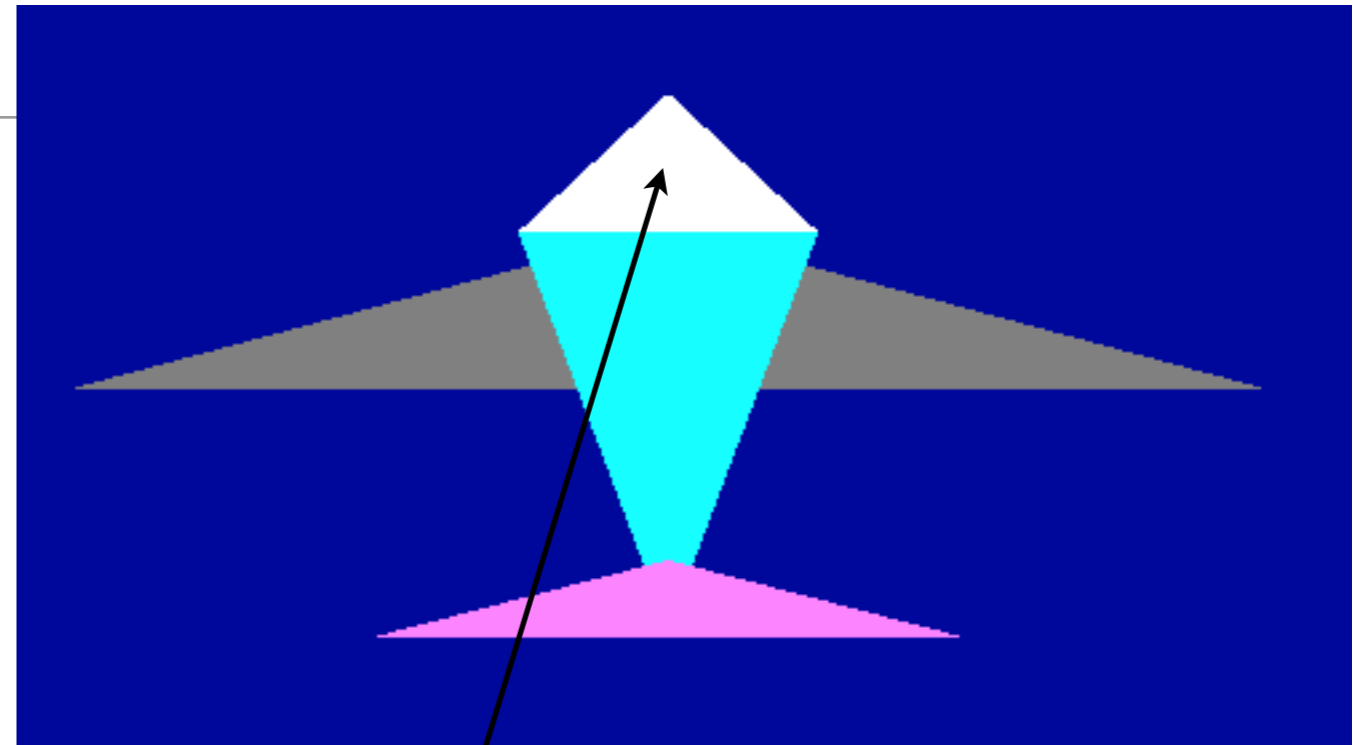
```
Vector3 noseCone[][3] =  
{ { Vector3 ( 0.0, 0.0, 6.0),  
  Vector3 ( -1.5, 0.0, 3.0),  
  Vector3 ( 1.5, 0.0, 3.0) },  
  { Vector3 ( 1.5, 0.0, 3.0),  
  Vector3 ( 0.0, 1.5, 3.0),  
  Vector3 ( 0.0, 0.0, 6.0) },  
  { Vector3 ( 0.0, 0.0, 6.0),  
  Vector3 ( 0.0, 1.5, 3.0),  
  Vector3 ( -1.5, 0.0, 3.0) }  
};
```

```
glBegin( GL_TRIANGLES);  
  glNormal3f(0.0f, -1.0f, 0.0f);  
  glVertex3f(0.0f, 0.0f, 60.0f);  
  glVertex3f(-15.0f, 0.0f, 30.0f);  
  glVertex3f(15.0f, 0.0f, 30.0f);  
glEnd();
```



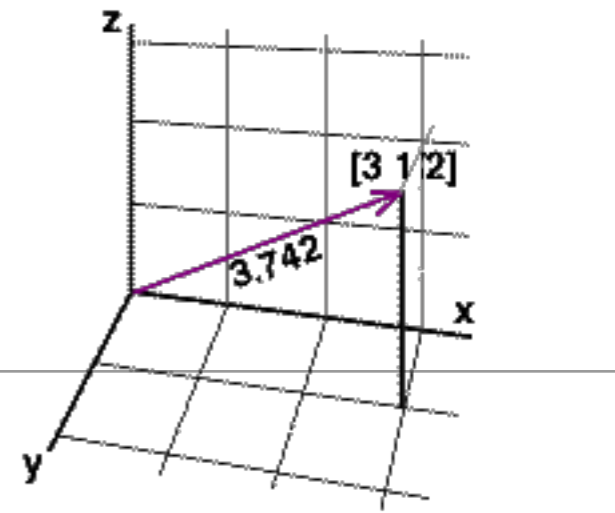
Recap: Winding

- Take special note of the order of the vertices in the jet's triangle.
- If you view this triangle being drawn from the direction in which the normal vector points, the corners appear counter clockwise around the triangle.
- This is called polygon winding.
- By default, the front of a polygon is defined as the side from which the vertices appear to be wound in a counterclockwise fashion.



```
glBegin( GL_TRIANGLES);  
    glNormal3f(0.0f, -1.0f, 0.0f);  
    glVertex3f(0.0f, 0.0f, 60.0f);  
    glVertex3f(-15.0f, 0.0f, 30.0f);  
    glVertex3f(15.0f, 0.0f, 30.0f);  
glEnd();
```

Unit Normals



- A unit normal is just a normal vector that has a length of 1.
- All surface normals must eventually be converted to unit normals.

$$\begin{aligned} \mathbf{v}[3 \ 1 \ 2] \\ \mathbf{x} = 3, \\ \mathbf{y} = 1, \\ \mathbf{z} = 2, \end{aligned}$$

- Normalization:

$$\begin{aligned} \text{length} &= \text{sqrt}((\mathbf{ax} * \mathbf{ax}) + (\mathbf{ay} * \mathbf{ay}) + (\mathbf{az} * \mathbf{az})) \\ \text{length} &= \text{sqrt}(9 + 1 + 4) = 3.742 \end{aligned}$$

- Calculate length: square each component, add them together, and take the square root.
- Divide each component of the normal by the length

$$\begin{aligned} \mathbf{x} &= 3.0 / 3.742 = \mathbf{0.802} \\ \mathbf{y} &= 1.0 / 3.742 = \mathbf{0.267} \\ \mathbf{z} &= 2.0 / 3.742 = \mathbf{0.534} \end{aligned}$$

$$\mathbf{v}[0.8, 0.27, 0.534]$$

OpenGL Normalize Computation

- Instruct OpenGL to convert your normals to unit normals automatically, by enabling normalization with `glEnable` and a parameter of `GL_NORMALIZE`::

```
glEnable(GL_NORMALIZE);
```

- This approach does, however, have performance penalties on some implementations.

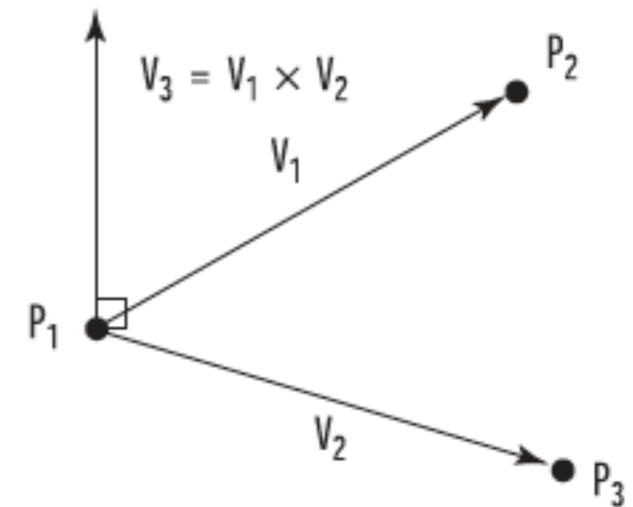
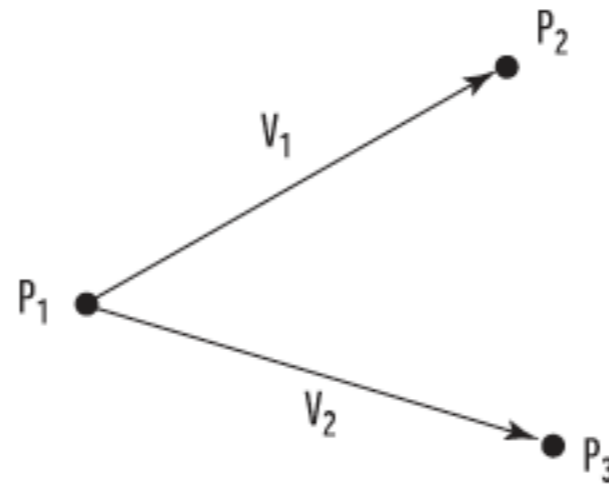
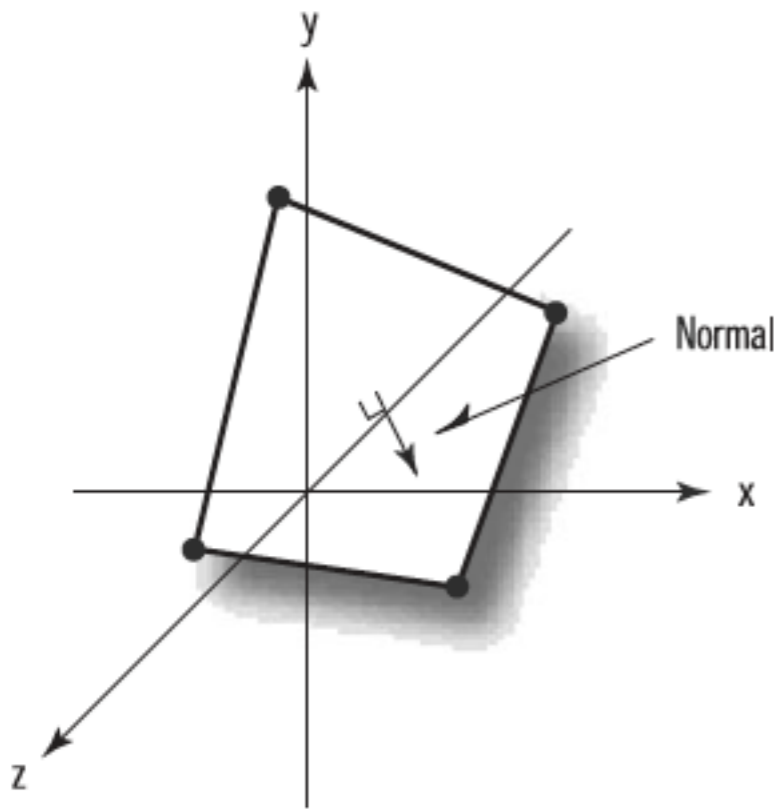
- May be better to calculate your normals ahead of time as unit normals instead of relying on OpenGL to perform this task.

- If applying scaling during a transformation, may need to rescale the normals to keep lighting effects consistent.

```
glEnable(GL_RESCALE_NORMALS);
```

Finding a Normal

- Take three points that lie in the plane of the polygon (P_1 , P_2 and P_3).
- Define two vectors: V_1 from P_1 to P_2 , and V_2 from P_1 to P_3 .
- Two vectors in three-dimensional space define a plane, so the cross product of V_1 and V_2 yields a vector is perpendicular to that plane - the Normal.



findNormal()

```
Vector3 findNormal(const Vector3& point1, const Vector3& point2, const Vector3& point3)
{
    Vector3 v1, v2;

    // Calculate two vectors from the three points. Assumes counter clockwise winding
    v1.X = point1.X - point2.X;
    v1.Y = point1.Y - point2.Y;
    v1.Z = point1.Z - point2.Z;

    v2.X = point2.X - point3.X;
    v2.Y = point2.Y - point3.Y;
    v2.Z = point2.Z - point3.Z;

    // Take the cross product of the two vectors to get the normal vector.
    Vector3 result;
    result.X = v1.Y * v2.Z - v2.Y * v1.Z;
    result.Y = -v1.X * v2.Z + v2.X * v1.Z;
    result.Z = v1.X * v2.Y - v2.X * v1.Y;
    return result;
}
```

Generate Normals

- Compute the normal and send to pipeline in advance of the vertices.

```
void render (Vector3 vectors[][3], int size)
{
    for (int i=0; i<size; i++)
    {
        glBegin(GL_TRIANGLES);
        Vector3 normal = findNormal( vectors[i][0], vectors[i][1], vectors[i][2]);
        glNormal3f(normal.X, normal.Y, normal.Z);
        vectors[i][0].render();
        vectors[i][1].render();
        vectors[i][2].render();
        glEnd();
    }
}
```